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## Data Representation, Logic, Huffman Coding, Binary Numbers

DUE: Friday March 17, 2017 @ the beginning of class Please staple all sheets together BEFORE class.

**Goal:** The purpose of this assignment is to get a little practice with binary numbers, think about representing data digitally, and review basic logic as the foundation of how computers compute.

#### Exercises:

#### **Binary Numbers**

- 1 Convert 10 base 10 to base 2.
- 2 Convert 16 base 10 to base 2.
- 3 Convert 32 base 10 to base 2.
- 4 Convert 217 base 10 to base 2.
- 5 Convert RGB color (128, 0, 255) to base 2. (\_\_\_\_, \_\_\_, \_\_\_)
- 6 Add 1101011 base 2 to 1011100 base 2, SHOW YOUR WORK.
- 7 Add 1011 base 2 to 110 base 2. SHOW YOUR WORK.

1101011	1011
+1011100	+110

8 What letters does this binary (base 2) data correspond to assuming it is in ASCII? 01001010, 01100001, 11110111, 00110000 = \_\_\_\_, \_\_\_\_, \_\_\_\_, \_\_\_\_

ASCII	0 0 0	0 0 0 1	0 0 1 0	0 0 1 1	0 1 0 0	0 1 0 1	0 1 1 0	0 1 1 1	1 0 0	1 0 0 1	1 0 1 0	1 0 1 1	1 1 0 0	1 1 0 1	1 1 1 0	1 1 1
0000	NU	s <sub>н</sub>	s <sub>x</sub>	<sup>в</sup> х	Ε <sub>T</sub>	EQ	А <sub>к</sub>	BL	в <sub>s</sub>	н <sub>т</sub>	L <sub>F</sub>	Υ <sub>T</sub>	FF	с <sub>к</sub>	s <sub>0</sub>	s <sub>I</sub>
0001	PL	D <sub>1</sub>	D_2	D_3	D_4	Νĸ	s <sub>y</sub>	ε <sub>Σ</sub>	с <sub>N</sub>	ЕМ	s <sub>B</sub>	Еc	Fs	G <sub>s</sub>	R <sub>S</sub>	U <sub>s</sub>
0010		!	"	#	\$	%	δc	1	(	)	*	+	,	-		/
0011	0	1	2	3	4	5	6	7	8	9	:	;	<	=	>	?
0100	@	A	в	С	D	Е	F	G	Η	I	J	K	L	М	Ν	0
0101	Ρ	Q	R	S	т	U	V	W	Х	Y	Z	[	$\backslash$	]	^	_
0110	`	a	b	С	d	е	f	g	h	i	j	k	1	m	n	0
0111	р	q	r	ន	t	u	v	W	х	У	Z	{		}	~	Рт
1000	<sup>8</sup> 0	<sup>8</sup> 1	<sup>8</sup> 2	<sup>8</sup> 3	I <sub>N</sub>	NL	s s	<sup>в</sup> s	н <sub>s</sub>	н <sub>ј</sub>	۲ <sub>s</sub>	PD	۴v	RI	s <sub>2</sub>	s <sub>3</sub>
1001	Рс	Р 1	۲z	s <sub>e</sub>	сc	м	s <sub>p</sub>	Е <sub>Р</sub>	а <sub>8</sub>	٩	۵ <sub>A</sub>	°s	s <sub>T</sub>	°s	Рм	Р
1010	<sup>A</sup> o	ī	¢	£	Ŷ	¥		S		©	o"	«	7	-	R	-
1011	0	±	2	3	-	μ	¶	•	u.	1	0	»	1⁄4	1/z	3/4	ż
1100	À	Á	Â	Ã	Ä	Å	Æ	Ç	È	É	Ê	Ë	Ì	Í	Î	Ï
1101	Ð	Ñ	Ò	Ó	Ô	Õ	Ö	×	Ø	Ù	Ú	Û	Ü	Ý	Þ	β
1110	à	á	â	ã	ä	å	æ	Ç	è	é	ê	ë	ì	í	î	ï
1111	ð	ñ	ò	ó	ô	õ	ö	÷	ø	ù	ú	û	ü	ý	Þ	ÿ

## Name:

## Logic

9 Complete the following truth tables.

# (a) NOT (p OR q)

p	q	p  OR  q	NOT $(p \text{ OR } q)$
1	1		
1	0		
0	1		
0	0		

(b) p AND (NOT q)

р	q	NOT $q$	p  AND (NOT  q)
1	1		
1	0		
0	1		
0	0		

## (c) p AND q AND r

р	q	r	p  AND  q	(p  AND  q)  AND  r
1	1	1		
1	0	1		
0	1	1		
0	0	1		
1	1	0		
1	0	0		
0	1	0		
0	0	0		

10 Using the 3 basic logic gates shown here, draw logic diagrams for the following logical statements.



- a NOT (P OR Q)
- b (A OR B) AND (NOT C)
- 11 Write the logical statement that corresponds to the following logic diagram.



#### Name:

Huffman Coding (Please attach a separate sheet of paper for the Huffman trees.)

12

a Generate a binary Huffman tree from the following letter frequencies for the word *bananarama*.

letter	b	a	n	r	m
frequency	1	5	2	1	1

b Using the binary Huffman tree you created for (a), give the binary Huffman encoding for the letter sequence *barn*.

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- a Generate a binary Huffman tree from the letter frequencies in the tongue twister: *She sells sea shells by the seashore*. Do not include the space character in your tree.
- b Using the binary Huffman tree you created for (a), give the binary Huffman encoding for the letter sequence *share*.
- 14 Create the Huffman tree that goes with the following frequency table.

letter	с	$\mathbf{s}$	r	t	е
frequency	1	2	3	4	7